# AB INITIO STRUCTURES OF ALLYLLITHIUM 

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## Summary

Complete optimization of classical and nonclassical allyllithium structures at the RHF/STO-3G level with subsequent RHF/4-31G and RHF/6-31G* calculations confirms the $C_{s}$ bridged species to have the lowest energy. The allyl fragment of this structure is significantly distorted from a planar arrangement in order to enhance bonding between the allyl anion HOMO (on C(1), C(3)) and the lithium $p$-orbital with axis parallel to $\mathrm{C}(1)-\mathrm{C}(3)$.

The structure of allyllithium has been the subject of considerable experimental [1,2] and theoretical [3-5] work. An earlier ab initio investigation involved only a partial geometry search [5] ***; we have not carried out complete optimization of bridged allyllithium, I ( $C_{s}$ ), and the syn and anti classical $C_{s}$ forms, II and III, at the minimal basis RHF/STO-3G [6a,b] level. Although not an energy minimum, an unsymmetrically bridged $C_{1}$ structure, $2-3 \mathrm{kcal} \mathrm{mol}^{-1}$ higher in energy than I was also investigated ${ }^{\dagger}$. The STO-3G optimum geometries of I-III, shown in Table 1, were then used for single point RHF/4-31G [8] and RHF/ $6-31 G^{*}$ [9] calculations. Total and relative energies are listed in Table 2. The

[^0]TABLE 1
CALCULATED (RHF/STO-3G) GEOMETRIES

| Parameter | I | II | III |
| :---: | :---: | :---: | :---: |
| Bond lengths |  |  |  |
| $\mathrm{C}(1) \mathrm{C}(2)$ | 1.401 | 1.315 | 1.312 |
| C(2) C(3) | 1.401 | 1.522 | 1.535 |
| C(2)Li | 2.006 | 2.527 | 3.046 |
| $\mathrm{C}(3) \mathrm{Li}$ | 2.039 | 1.961 | 2.025 |
| C(1) H(I) | 1.084 | 1.098 | 1.081 |
| C(1) İ(2) | 1.075 | 1.080 | 1.081 |
| C(2) $\mathrm{H}(3)$ | 1.090 | 1.094 | 1.084 |
| C(3) 15(4) | 1.084 | 1.085 | 1.087 |
| C(3) H(5) | 1.075 | 1.085 | 1.087 |
| Bond angles |  |  |  |
| $\mathrm{C}(1) \mathrm{S}(2) \mathrm{C}(3)$ | 123.0 | 126.0 | 123.5 |
| C(2) C(3)Li | 82.6 | 92.2 | 117.0 |
| $\mathrm{C}(2) \mathrm{C}(1) \mathrm{H}(1)$ | 116.1 | 123.4 | 122.0 |
| C(2) C(1) H(2) | 118.6 | 124.0 | 122.5 |
| C(1) $\mathrm{C}(2) \mathrm{H}(3)$ | 107.6 | 116.5 | 117.6 |
| C(2) ©(3) H(4) | 116.1 | 107.5 | 107.3 |
| $\mathrm{C}(2) \mathrm{C}(3) \mathrm{FI}(5)$ | 118.6 | 107.5 | 107.3 |
| Out-of-plane angles ${ }^{\text {a }}$ |  |  |  |
| C(2)Li | 46.9 | 0.0 | 0.0 |
| C(1) H(1) | -31.1 | 0.0 | 0.0 |
| C(1) E (2) | -3.0 | 0.0 | 0.0 |
| C(2) H(3) | 11.1 | 0.0 | 0.0 |
| C(3) H(4) | -31.1 | 56.4 | 55.5 |
| C(3) H(5) | -3.0 | -56.4 | -55.5 |

a Out-of-plane angles are positive when the givan bond is above the $C(1) C(2) C(3)$ plane and negative below the plane.
bridged $C_{s}$ structure, I, proved to be most stable at all levels. This is consistent with previcus work [5]. The anti classical species proved to be the least stable in all the calculations. The relative energies of I, II and III are close: 0,16 and 18 $\mathrm{kcal} \mathrm{mol}^{-1}$, respectively, at both RHF/4-31G and RHF/6-31G* (Table 2).

It should be emphasized that II and III were optimized within the constraints of $C_{5}$ symmetry, i.e., all non-hydrogen atoms were held in a plane. Were this restriction to be removed, both II and III would probably collapse to I, without

TABLE 2
TOTAL AND RELATIVE ENERGIES OF ALLYLLITHIUM SPECIES I-III AT THE RHF/STO-3G OPTEMIZED GEOMETRIES

| Structure | Total energies (a.u.) |  |  | Relative energies (kcal mor ${ }^{\text {- }}$ ) |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | STO-3G | 4-31G | 6-31G* | STO-3G | 4-31G | 6-31G* |
| I, bridged | -122.39929 | -123.74560 | -123.91360 | 0.0 | 0.0 | 0.0 |
| II, ss'n | -122.35659 | -123.72025 | -123.88862 | 26.8 | 15.9 | 15.7 |
| III, anti | -122.34928 | -123.71733 | -123.88419 | 31.4 | 17.7 | 18.5 |

encountering a significant energy barrier. Thus, I not only is the most stable form, but alse may be the sole minimum on the $\mathrm{C}_{3} \mathrm{H}_{5} \mathrm{Li}$ potential energy surface. Unsuccessful searches were made for other minima, but these were not exhaustive.


I



The structure of the anti classical species, III, gave no unexpected geometrical features upon optimization. However, the syn classical isomer collapsed to a "semi-bridged" form (II) with a CCLi angle of $92.2^{\circ}$. In the bridged $C_{s}$ isomer, I, the geometry of the $\mathrm{C}_{3} \mathrm{H}_{5}$ moiety closely approaches that of the allyi anion ( $C_{2 y}$ ) [5], but the CCC angle diminishes from $132.7^{\circ}$ to $123.3^{\circ}$, presumably because of improved $\mathrm{C}(1) \mathrm{Li}$ and $\mathrm{C}(3) \mathrm{Li}$ overlap. The methylene CH bonds are all somewhat bent down below the CCC plane ( Li being above). The central Cis bond ( $\mathrm{C}(2) \mathrm{H}(3)$ ) bends towards lithium so that $\mathrm{H}(3)$ lies above the CCC plane.

The energy of the isodesmic ex:hange reaction 1 provides estimates of the relative stability of allyl- and ethyl-lithium structures. These are given in Table 3*.

$$
\begin{equation*}
\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{Li}+\mathrm{CH}_{3} \mathrm{CH}=\mathrm{CH}_{2} \rightarrow \mathrm{C}_{3} \mathrm{H}_{5} \mathrm{Li} \div \mathrm{C}_{2} \mathrm{H}_{6} \tag{1}
\end{equation*}
$$

At the RHF/6-31G* level, the energies are negative for all three species. For the anti classical isomer III, the value is very small, indicating no significant double bond inductive effect relative to ethyllithium. However, there is a somewhat larger stabilization ( $3.2 \mathrm{kcal} \mathrm{mol}^{-1}$ ) with the syn classical form II. This arises partly by donation from the double bond $\pi z$ orbital to the empty $p \pi z$ orbital on lithium, an interaction which also leads to the closing of the CCLi angle.

The high additional stabilization in the bridged form I of $18.9 \mathrm{kcal} \mathrm{mol}^{-1}$ (RHF/6-31G*) can be attributed to several stabilizing features of this structure. An important effect, which has been discussed previously [3-5], is the bonding overlap between the highest occupied molecular orbital (HOMO) of an allyl

[^1]TABLE 3
CALCULATED ENERGIES FOR EQUATION I

| $\mathrm{C}_{3} \mathrm{H}_{5} \mathrm{Li}$ stracture | $\Delta E\left(\mathrm{kcal/mole)}{ }^{\text {a }}\right.$ |  |  |
| :--- | :---: | :---: | :---: |
|  | RHF/STO-3G | RHF/4-31G | RHF/6-31G* |
| I, bridged | -30.8 | -18.3 | -18.9 |
| Ir, syn | -4.0 | -2.4 | -3.2 |
| III, anti | +0.6 | -0.6 | -0.4 |

$a_{\text {All calculations at the STO-3G optimized geometries given in Table 1; other data used are taken from }}$ zefs. 10-12.
anion moiety and the vacant $\mathrm{Li}^{+} p x$-type orbital (with axis parallel to $\mathbf{C ( 1 ) C ( 3 ) )}$. This type of bonding was first suggested by X-ray crystal structures of benzyl and related lithium compounds [13]. As lithium is the acceptor in such an interaction, the effect is to reduce the overall charge transfer from lithium to allyl., The interaction is enhanced by inclination of the lobes of the $C(1), C(3) p \pi$ orbitals towards lithium. The bending down of the methylene hydrogen accentuates such inclination. Indeed, this bending results in a destabilization of the $\mathrm{C}(1) \mathrm{C}(2) \mathrm{C}(3) \pi$ bonding orbital by 0.0103 a.u. but a stabilization of the HOMO by 0.0294 a.u. relative to the structure with $\mathrm{C}_{3} \mathrm{H}_{5}$ planar. Similarly, the $\mathrm{C}(2) \mathrm{H}(3)$ bond bends up to further increase HOMO bonding between $p x$ on lithium and the twisted $p$-orbitals of $C(1)$ and $C(3)$. This type of interaction is further demonstrated by the Mulliken population analysis for $I$, shown in Table 4. Lithium is clearly bonded to $C(1)$ and $C(3)$, although $C(2)$ is the closest carbon. At RHF/ STO-3G, C(2) and Li are actually antibonding.

The recently reported enthaipies of reaction of allyllithium and ethyllithium with ethanol in ether [14] afford a means of evaluating the energy of reaction 1 experimentally; a value of $-13.7 \pm 2.6 \mathrm{kcal} \mathrm{mol}^{-1}$ is obtained. The agreement with the calculated values (Table 3) is fortuitous, since the experimental measurements are complicated by different degrees of association of ethyllithium and of allyllithium and by possible differences in solvation energies. The calculations, of course, refer to isolated species at 0 K .

The protori NMR spectrum of allyllithium [15] shows an ABB'CC' pattern

TABLE 4
MULLIKEN POPULATION ANALYSIS FOR $C_{S}$ ALLYLLITHIUM, I

|  |  | RHF/STO-3G | RHF/4-31G |
| :--- | :--- | :--- | :--- |
| Net atomic charges | $\mathrm{C}(1)$ | -0.197 | -0.518 |
|  | $\mathrm{C}(2)$ | 0.013 | 0.146 |
|  | Li | 0.110 | 0.439 |
| Total overlap populations | $\mathrm{C}(1) \mathrm{C}(2)$ | 0.983 | 0.801 |
|  | $\mathrm{C}(1) \mathrm{Li}$ | 0.310 | 0.300 |
|  | $\mathrm{C}(2) \mathrm{Li}$ | -0.066 | 0.030 |
|  | $\mathrm{C}(2) \mathrm{Li}\left(P_{\pi}\right)^{a}$ | 0.227 | 0.212 |
| Dipole moment $(D)$ |  | 0.922 | $2.820^{b}$ |

[^2]at $-87^{\circ} \mathrm{C}$ but coalesces to $\mathrm{AB}_{4}$ at higher temperatures. This behavior has been attributed to exchange of $H(1)(H(4))$ and $H(2)(H(5))$ due to rotation about the $\mathbf{C}(1) \mathrm{C}(2)(\mathbf{C}(2) \mathrm{C}(3))$ bond. The experimental activation energy for this process is $10.5 \pm 2 \mathrm{kcal} \mathrm{mol}^{-1}$ in tetrahydofuran [15]. Since organolithium compounds are known to be strongly solvated and/or associated, our calculations on isolated monomers can only be expected to approximate this value. Nevertheless, it is revealing to consider the mechanism of HH exchange. If the metal and allyl fragment are bound to the same degree in ground and transition states, as would be the case in a dissociated species, the barrier should be independent of the metal and should be approximated by that of the allyl anion itself ( $29 \mathrm{keal} \mathrm{mol}^{-1}$ at 4-31G) [16]. If the metal is bound to a greater extent in the rotational transition state than in the ground state, a reduced barrier and a dependency on the metal would result. Both are found experimentaliy; the rates of cis-trans stereomutation of crotyl(1-methylallyllithium, -sodium, -potassium, and -cesium increase markedly in that order [2].

Our calculaied barrier for allyllithium, approximated by the 6-31G* energy difference between I and II (III is higher in energy), is 16 or $13 \mathrm{kcal} \mathrm{mol}^{-1}$ lower than that calculated for the allyl anion at the same ievel [16]. Preliminary calculations on allylsodium indicate the barrier to be higher than that for allyllithium.

A reasonable interpretation of these observations focuses on the degree of covalent character in the metal to carbon bonding. The larger and more electropositive alkali metals are not expected to stabilize the more localized transition state (e.g., II) as well as the delocalized ground state (e.g. I). Lithium-carbon bonding, because of partial covalent character in II, reduces the rotational barriers appreciably. However, when it is recalled that the methyl rotation barrier in propene is only $2 \mathrm{kcal} \mathrm{mol}^{-1}$ (the barriers in the usual methyl-substituted propenes are not much larger), the large degree of ionic character of allyllithium is apparent.

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    *** The lowest RHF/STO-3G energy of allylithium reported was $\mathbf{- 1 2 2 . 3 7 4 1}$ a.u. for a structure with $C_{s}$ symmetry. The RHF/4-31G total energy for the reported $\mathrm{C}_{3} \mathrm{H}_{5}{ }^{-}$geometry is $\mathbf{- 1 1 6 . 2 2 6 3 9}$ a.u.
    $\dagger$ An unsymmetrically bridged structure, IV, was obtained when complete optimization of a classical allyllithium (Li initially perpendicular to the CCC plane) was carried out by cyclic variation of all parameters one at a time [5a]. Our interest in this problem arose when we found IV to have a lower energy than that reported for I by the earlier workers, Although IV met our criteria for an energy minimum (total energy change was less than $10^{-5}$ a.u. ( $6 \times 10^{-3} \mathrm{kcal}$ mor ${ }^{-1}$ ) per complete cycie), (multiplayer search) Fletcher et al. [7] showed this conclusion to be incorrect as it led to I.

[^1]:    * RHF/STO-3G. RHF/4-31G and RHF/6-31G* total energies for ethyllithium are -84.99605, -85.92765 and -86.04106 a.u., respectively, at the STO-3G optimum geometry [10].

[^2]:    ${ }^{\sigma}$ The $\pi$ component of the total overlap. ${ }^{b}$ Value 2.868 debyes at RHF/6-31G* level.

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